

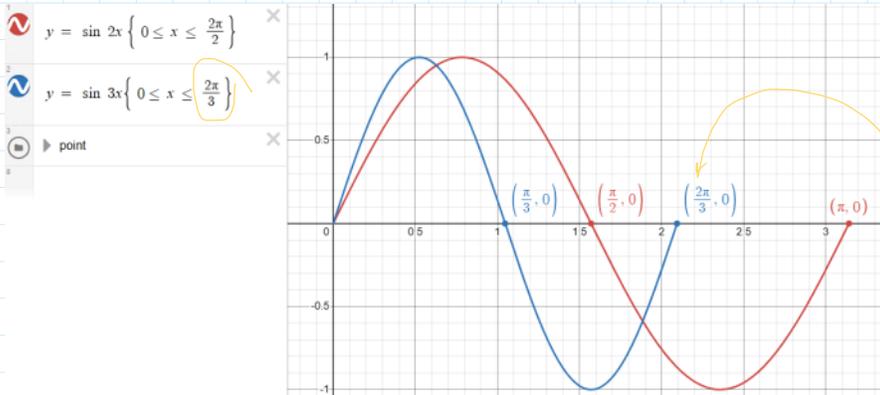
13. The second harmonic in sound is given by $f(x) = \sin 2x$, while the third harmonic is given by $f(x) = \sin 3x$. Sketch the curves and compare the graphs of the second and third harmonics for $-2\pi \leq x \leq 2\pi$.

sketch = always by hand

Did You Know?

A harmonic is a wave whose frequency is an integral multiple of the fundamental frequency. The fundamental frequency of a periodic wave is the inverse of the period length.

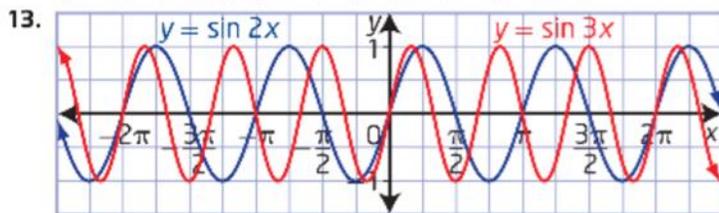
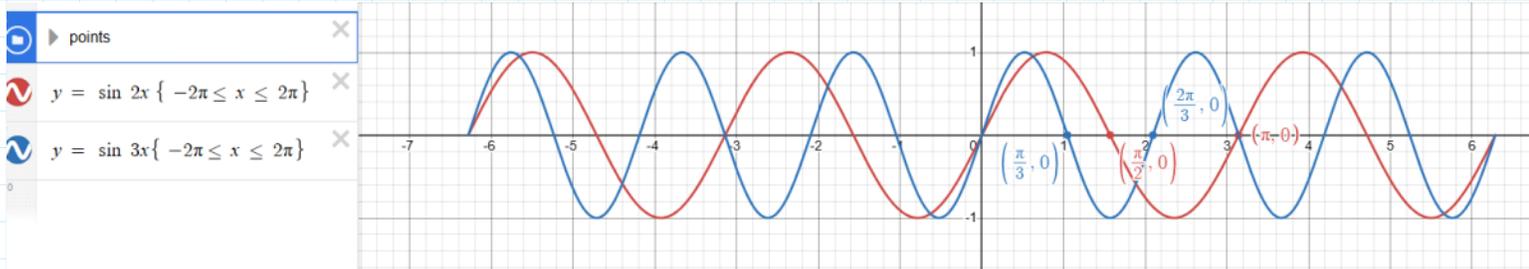
<https://www.desmos.com/calculator/zt4nfnqkh>



make a table of critical points
 x- intercepts
 max/min
 y-intercepts
 and apply the stretched to x
 red: H stretch by a factor of 1/2
 blue: H stretch by a factor of 1/3

x -> x *factor

ex: $2\pi \rightarrow 2\pi \cdot (1/3)$



The amplitude, maximum, minimum, y-intercepts, domain, and range are the same for both graphs. The period and x-intercepts are different.