

8. Determine the product of $g(x) = \frac{1}{1+x}$ and $h(x) = \frac{1}{3+2x}$. Then, state the domain of the combined function.

$$f(x) = \frac{1}{1+x} \cdot \frac{1}{3+2x}$$

NPV $x = -1$

NPV: $x = -\frac{3}{2}$

$$(1+x)(3+2x) = 3+2x+3x+2x^2 = 2x^2+5x+3$$

$$f(x) = \frac{1}{(1+x)(3+2x)} = \frac{1}{2x^2+5x+3}$$

this is
const
parabola form

the graph of the function is usefull in finding the range

w/ two roots: $x = -1$ & $x = -\frac{3}{2} = -1.5$

The domain is the commonality of the two domains excluding the NPV-s values.

$$D_g: \{x \mid x \neq -1, x \in \mathbb{R}\}$$

$$D_h: \{x \mid x \neq -\frac{3}{2}, x \in \mathbb{R}\}$$

$$D_h = \left\{ x \mid x \neq -\frac{3}{2}, x \in \mathbb{R} \right\}$$

The common domain is

$$D_f = \left\{ x \mid x \neq -1 \text{ \& } x \neq -\frac{3}{2}, x \in \mathbb{R} \right\}.$$

$$f(x) = \frac{1}{(1+x)(3+2x)} = \frac{1}{2x^2 + 5x + 3}$$

verify in Desmos:

<https://www.desmos.com/calculator/ynmytm9cip>